Full Length Article

Parametrizing nonbonded interactions between silica and water from first principles

H. Gokberk Ozcelik\(^a\), Yigit Sozen\(^b\), Hasan Sahin\(^b\), Murat Barisik\(^{a, *}\)

\(^a\) Department of Mechanical Engineering, Izmir Institute of Technology, IZMIR, 35430, Turkey
\(^b\) Department of Photonics, Izmir Institute of Technology, IZMIR, 35430, Turkey

1. Introduction

In recent years, various forms of silica materials have been used in a wide range of nanotechnologies such as DNA analyzers [1], targeted drug delivery [2], biological/chemical agent detectors [3], micro/nano chips [4], atomic force microscopes [5] and nano-membranes [6]. Molecular level interactions between solid domains and liquids define the operation of these applications and a significant amount of effort has been put towards understanding the interface coupling between silica nanostructures and water.

While the experiments are challenging and expensive, molecular dynamics (MD) calculations have been a robust and reliable tool to provide insight to the nano-scale world. However, success of MD simulation is strictly related to the functions that are used to model interatomic potentials. A number of successful force fields have been proposed to model silica. For example, intramolecular interactions between silicon and oxygen atoms can be accurately predicted by using well-validated BKS model of van Beest et al. [7] or by Tersoff potential modified for silica systems by Munetoh et al. [8]. On the other hand, calculating interactions of Silica with other molecules is still challenging. Recently, complex algorithms such as “Reactive force field for silica” (ReaxFFSiO) proposed by van Duin et al. [9] was further examined by Fogarty et al. [10] and practiced by many [11,12] to resolve surface chemistry of silica. In the majority of current literature, the nonbonded interactions are modeled using the two-body Lennard-Jones (LJ) potential and Coulomb’s law. In such an approach, the required LJ potential parameters between pairs of non-identical molecules are frequently calculated from the parameters of the pair of identical molecules by using simple mixing rules [13]. For instance, the Lorentz–Berthelot (LB) mixing rule utilizes arithmetic mean for molecular diameter and geometric mean for the potential strength. However, the interaction parameters between identical molecules are optimized for a bulk material system, which may need to be re-parameterized for the interaction of nonidentical pairs instead of using mixing rules. For example, MD wetting simulations using LB mixing rule fails to capture wetting behavior of silicon surface since the interaction parameters between oxygen and silicon atoms were overestimated [14]. Multiple authors indicated their concerns and proposed ways to calculate the interaction parameters of non-identical molecules accurately [13–18].

One methodology is the measurement of water contact angle to
define the interactions of water with corresponding surface. For example, interaction parameters between oxygen atoms of water and silicon atoms of surface was tuned to recover experimentally measured wetting angle on a clean silicon surface [14]. Such methodology yielded very accurate interface modeling for graphene [19] and silicon [14] surfaces. A similar idea was employed for silica by Cruz-Chu et al. [20]; however, instead of changing the interface interactions parameters, the authors changed the potential depth of silicon-silicon interactions to tune the water and silica interaction parameters calculated from mixing rule. Such perspective still suffers from problems arising from mixing rule; the interaction parameters are not transferable to any other MD simulations of silica/water systems.

Instead, interaction parameters between water and silica can be predicted from first principle calculations. Multiple studies were dedicated to develop the nonbonded interaction parameters for an accurate description of coupling between water and various materials, such as molybdenum disulfide [21], hexagonal boron nitride [22] and graphitic carbon [23]. Parametritization of nonbonded interactions is an up-to-date research and a very recent article about current perspectives can be found in [24]. The most commonly used quantum mechanical approach is the Kohn-Sham density functional theory (DFT) [15,25] which has been well-validated. Although, there are many criticisms about the accuracy of DFT, failures are mostly associated with the “density-functional approximation” [26]. Furthermore, due to exchange-correlation functionals required to model interactions between electrons, standard DFT calculation fails to describe long-range electron interactions developing the dispersion or the van der Waals (vdW) forces [27]. Simply, the standard functionals only calculate short-range local properties and do not consider instantaneous fluctuations in electron density. Therefore, additional corrections are needed to capture vdW forces in DFT calculations. A vast number of studies were dedicated to develop DFT-based dispersion techniques. With an interesting analogy, Klimes and Michaelides tried to classify and rank the dispersion correction models and compared them with corresponding experimental measurements as presented in Table 1. The GGA-D3 with Becke-Jonson damping yielded results closest to experimental values.

Similarly, the GGA-D3 with Becke-Jonson calculated 4.919 Å lattice constant for α-quartz silica, which is almost identical to experimentally measured constant as 4.916 Å [42]. Therefore, DFT-D3 method with Becke-Jonson damping was used as the correction onto GGA for the identification of electron-electron correlation in order to get more accurate vdW interactions between H2O and silica surface. The cut-off kinetic energy for each plane wave basis was kept limited to 500 eV and the total energy difference among two electronic steps was specified as 10−5 eV as the convergence criterion. Gaussian smearing method was used to obtain partial occupancies with a width of 0.05 eV. Optimization calculations of single silica and water structures were performed until the pressure falls below 1 kbar along the x, y and z directions. To generate (1 0 0) surface of silica and to avoid interactions between adjacent slabs, a 35 Å height vacuum space was created along the x axis. A conventional cell of silica with lattice parameter of a = 9.83 Å and b = 10.70 Å was used to avoid possible interaction of water with itself through the periodic boundary conditions. For construction of the truncated silica surface slab, dangling bonds at the lowermost layer were terminated by H atoms. The 8 Å thick slab was found adequate to mimic the 3D bulk structure.

### 2. Methodology

#### 2.1. Details of DFT calculations

To investigate the interactions between silica surface and water molecule; first principle calculations were performed using the projector augmented wave (PAW) method [33,34] implemented in the Vienna ab-initio simulation package (VASP). Exchange correlation potentials of the structure were defined with the Perdew-Burke-Ernzerhof (PBE) model of Generalized Gradient Approximation (GGA) functional [35]. Earlier versions for electron correlation with dispersion forces were found overemphasizing the binding energies [22,36,37]. Specifically, DFT-D2 following Grimme’s method [28] and PBE-TS following the methods of Tkatchenko and Scheffler [30] yielded high interaction parameters which underestimated the water wetting angles. Through the several tests we performed, DFT-D3 method with Becke-Jonson damping [38] gave consistent results with the experimental ones. For example, we calculated the interlayer distance (t) of bilayer graphene and the lattice parameter (a) of bulk silicon crystal using different dispersion correction models and compared them with corresponding experimental measurements as presented in Table 1. The GGA-D3 with Becke-Jonson Damping yielded results closest to experimental values.

<table>
<thead>
<tr>
<th>t (Å)</th>
<th>a (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Experimental</td>
<td>3.40 [39]</td>
</tr>
<tr>
<td>LDA</td>
<td>3.29</td>
</tr>
<tr>
<td>GGA</td>
<td>3.48</td>
</tr>
<tr>
<td>GGA-D2</td>
<td>3.26</td>
</tr>
<tr>
<td>GGA-D3 (Zero Damping)</td>
<td>3.44</td>
</tr>
<tr>
<td>GGA-D3 (Becke Jonson Damping)</td>
<td>3.40</td>
</tr>
<tr>
<td>GGA-TS</td>
<td>3.36</td>
</tr>
<tr>
<td>GGA-MBD@rsSCS</td>
<td>4.17</td>
</tr>
<tr>
<td>GGA-D06C</td>
<td>4.03</td>
</tr>
</tbody>
</table>

#### 2.2. Details of MD calculations

MD simulation of a water nanodroplet on silica surface was performed to test the interaction parameters determined from DFT. Simulation was 4 nm × 16 nm × 10 nm size in x × y × z-directions. Periodicity condition was applied at x and y directions. A reflecting wall boundary condition was applied 8 nm above silica surface which flips the velocity of water molecules and returns them back to simulation.
The molecules at the lowest layer of silica slab were fixed to their original position to keep the volume constant. Tersoff style silica potential [8] was employed to model α-quartz structure. LAMMPS (Large-scale Atomic/Molecular Massively Parallel Simulator) Code [43] was used as the MD solver. A hemi-cylindrical droplet was formed with 1280 water molecules. SPC/E model was chosen as the water model due to simplicity and computational cost. Accordingly, length of OH bond was constrained with SHAKE algorithm as 0.1 nm and to simplify and computational cost. Accordingly, length of OH bond was constrained with SHAKE algorithm as 0.1 nm and to simplify and computational cost.

From SPC/E model, the interaction parameters between dissimilar molecules, it is a common practice through MD studies to estimate these parameters using various forms of mixing rules. For example, for the silicone-oxygen interactions, parameters can be calculated by the LB mixing rule given as, 

\[
\Phi(r_{ij}) = 4\varepsilon\left(\frac{\sigma}{r_{ij}}\right)^{12} - \left(\frac{\sigma}{r_{ij}}\right)^6
\]

where \(r_{ij}\) is the intermolecular distance, \(\varepsilon\) is the depth of the potential well, \(\sigma\) is the molecular diameter. The interaction parameters for similar molecular pairs used in the simulations are given in Table 2. Interaction parameters between similar materials were taken from the corresponding model. For example, interaction parameters between silica atoms were defined by the Tersoff model while interactions between water molecules were from SPC/E model. On the other hand, for the interaction parameters between dissimilar molecules, it is a common practice through MD studies to estimate these parameters using various forms of mixing rules. For example, for the silicone-oxygen interactions, parameters can be calculated by the LB mixing rule given as,

\[
s_{\text{Si-O}} = \frac{s_{\text{Si-Si}} + s_{\text{O-O}}}{2}, \quad s_{\text{Si-O}} = \sqrt{s_{\text{Si-Si}}} \times s_{\text{O-O}}
\]

Using the corresponding parameters given in Table 2, the L-B mixing rule predicts the interaction parameters \(s_{\text{Si-O}} = 2.6305\ \text{Å}\) and \(s_{\text{Si-O}} = 0.12088\ eV\). However, our earlier wetting study based on MD measured contact angles of water nanodroplets showed that interaction parameters from LB do not create the wetting behavior of a clean silicon surface. Instead, the experimentally measured hydrophobic behavior of silicon surfaces can be recovered when the silicon-oxygen interaction strength is 12.5% of the value predicted by the LB mixing rule [14]. For such a case, we employed this previously proposed interaction strength value for the interaction between \(\text{Si}_{\text{Silica}}\) and \(\text{O}_{\text{Water}}\) as \(s_{\text{Si-O}} = 0.01511\ eV\), while the interaction parameters for \(\text{O}_{\text{Silica}}\cdot\text{O}_{\text{Water}}\) were determined from DFT calculations.

The Verlet algorithm was applied to integrate Newton’s equation of motion with a time step of 0.001 ps. At the beginning of simulations, Maxwell-Boltzmann velocity distribution was assigned for all molecules at 300 K. Nose-Hover style NVT ensemble was applied to keep the temperature at 300 K. Simulations are carried out 2 × 10^6 timesteps (2 ns) to reach an isothermal steady state. After that, microcanonical ensemble was applied to obtain averaging of the desired properties for 6 × 10^6 timesteps (6 ns). Averaging is performed with 5 ps intervals. Two different binning were used for averaging. Due to the hemi-cylindrical droplet shape, long rectangular prisms with the size of 0.1 nm × infinity × 0.1 nm along x, y, and z directions were used to resolve droplets. On the other hand, slab bins with infinity × infinity × 0.01 nm along x, y, and z directions were used to resolve silicon domain.

### 3. Results and discussions

The ab initio total energy optimization calculations were performed to estimate the total interaction energies between a water molecule and silica (1 0 0) surface of alpha quartz, to develop force field parameters for LJ potential model. First, we investigated how the single water molecule was adsorbed on the different sites of the silica surface. In order to find the possible adsorption sites, the water molecules were located at various points on silica (1 0 0) surface and geometric optimizations were performed for each.

Possible adsorption sites are represented in Fig. 1(a). While the molecule that was located on the uppermost silicon atom retained its position (site-1), molecules located above the center of the valley and between the closest topmost silicon atoms slightly shifted their initial points (site-2 and site-3). Even though site-2 and site-3 are similar in position, depending on the orientation of the water molecule, site-2 and site-3 differentiated. Site-2 and site-3 developed much higher binding energies than site-1; so that site-1 is more suitable to represent non-bonded interactions. Consequently, the approaching water molecules firstly terminated the lattice points around site-2 and site-3 which resulted in strong binding energies. After the saturation of these highly interactive sites, water molecules settled onto points similar to site-1. As an arbitrary chosen adsorption site, site-4 was also taken into account.

### Table 2

<table>
<thead>
<tr>
<th>Molecule Pair</th>
<th>(\sigma) (Å)</th>
<th>(\varepsilon) (eV)</th>
<th>(q) (e)</th>
</tr>
</thead>
<tbody>
<tr>
<td>O–O</td>
<td>3.166</td>
<td>0.006739</td>
<td>−0.8476</td>
</tr>
<tr>
<td>H–H</td>
<td>0</td>
<td>0.4238</td>
<td></td>
</tr>
<tr>
<td>Si–O [14]</td>
<td>2.633</td>
<td>0.01511</td>
<td>0</td>
</tr>
</tbody>
</table>

### Results and discussions

(a) Location of the Sites

(b) Site-1

(c) Site-2 and Site-3

(d) Site-4

Fig. 1. (a) Top view of silica (1 0 0) surface and the adsorption sites for water molecules after structural optimizations. (b)–(d) are side views of site-1, site-2 and site-3, and site-4, respectively. Orange colored atoms represent the topmost silicon atoms. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
Before starting the indentation process, a water molecule was placed above the topmost silicon atom at least 7 Å and moved to the surface step by step in a controlled manner to obtain the exact potential energy curves of each site. In each step of indentation, oxygen of water molecule was fixed, while hydrogen atoms were free to move with respect to the position of oxygen atom to find their most favorable adsorption configuration at each step. It was seen that upon indentation, binding energies varied on each site. The interaction potential profile of site 2 and site-3 showed comparably strong interaction at the silica-water interface (Fig. 2). Their energies were calculated to be 592 meV and 436 meV. Besides, lower binding energies were observed from site 1 and site 4. Their binding energies were 124 meV (site 1) and 0.168 meV (site 4).

Next, interaction energy between water molecule and silica surface was extracted by subtracting energies of water molecule and silica structure from total energy of systems. Fundamentally, current water and silica system interacted through dispersive forces and these vdW forces developed due to the interactions of oxygen of water with the silicon and oxygen atoms of silica. Through such perspective, we hypothesized that obtained potential energy curves are in the form of L-J function as,

\[
\Delta E = \sum_i 4\epsilon_{Si-O_w} \left( \frac{r_{Si-O_w}}{\sigma_{Si-O_w}} \right)^{12} - \left( \frac{r_{Si-O_w}}{\sigma_{Si-O_w}} \right)^6 + \sum_i 4\epsilon_{O-Si} \left( \frac{r_{O-Si}}{\sigma_{O-Si}} \right)^{12} - \left( \frac{r_{O-Si}}{\sigma_{O-Si}} \right)^6
\]

where subscripts Si, O_w and O denote silicon atoms in silica, oxygen atoms in silica and oxygen atom of the water molecule, respectively. The first term on the right-hand side calculates interactions between the oxygen of water with every Si atom in silica while the second term of right side calculates interactions between the oxygen of water with every oxygen of silica. Eq. (3) requires four parameters, interaction strengths and diameters. The well-known practice is to estimate interaction diameters as the mean of vdW diameters of corresponding atoms. However, using a mixing rule to determine interaction strength between dissimilar atoms creates inaccurate interface coupling, as we described in earlier sections. Alternatively, we employed interaction strength between silicon and oxygen of water from our earlier study [14] and estimate interaction strength between oxygen of silica and oxygen of water from DFT results presented in Fig. 2. For such a case, pairwise interaction of dissimilar oxygen atoms was extracted from total energies for every site. For every site of silica surface, we applied L-J potential calculations between water and silica defined by Eq. (3) as a curve fit onto the potential energy curves from DFT calculations. Resulting interaction strength parameters between oxygen of water and oxygen of silica are given in Table 3. Interaction energies calculated from these interaction strengths are given in Fig. 3. Very high binding energies were measured at site 2 and 3 is due to tendency for bond formation. At these sites, interaction strength values were measured very high; maximum interaction strength was extracted from site 3 although maximum binding energy is obtained from site 2. Since binding energy depends on local electron density but, due to additive pairwise potentials, interaction strength is affected by orientation of atoms and distance between pairs. Thus, site that have maximum binding energy and site that maximum interaction strength could

![Fig. 2. Energy vs distance curves of different sites on alfa quartz (1 0 0) surface and binding energies of the sites.](image)

![Fig. 3. Potential energy between oxygen of water and oxygen atoms of silica as a function of separation distance.](image)

![Fig. 4. (a) Snapshot of domain at the beginning of molecular dynamics simulation. Silicon, oxygen and hydrogen atoms presented in yellow, red and white, respectively. (b) Schematic illustration of water droplet and its contact angle. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)](image)

<table>
<thead>
<tr>
<th>Site 1</th>
<th>Site 2</th>
<th>Site 3</th>
<th>Site 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>ε_{Si-O_w}</td>
<td>0.012</td>
<td>0.075</td>
<td>0.38</td>
</tr>
</tbody>
</table>

Table 3: Molecular interaction parameters fitted for O-O_w water model.
such approach yields interface coupling di
models from the interaction parameters of identical pairs. However, interaction of dissimilar atoms are frequently estimated using mixing (MD) simulations. In the current literature, required parameters for the nonbonded molecular interactions parameters for Molecular Dynamics calculated using density functional theory (DFT), in order to provide

4. Conclusion

Binding energy between a silica slab and a water molecule was calculated using density functional theory (DFT), in order to provide nonbonded molecular interactions parameters for Molecular Dynamics (MD) simulations. In the current literature, required parameters for the interaction of dissimilar atoms are frequently estimated using mixing models from the interaction parameters of identical pairs. However, such approach yields interface coupling different than the experimentally measured behavior. Instead, required interaction parameters can be predicted by DFT. But, in the standard DFT calculations, dispersion forces are not considered in electron correlations so that additional correction models are required. These dispersion correction models are still under development and there are multiple models at different levels of sophistications in literature. We tested different dispersion correction models to calculate structural parameters of bilayer graphene, silicon and silica. The Becke-Johnson model for long-range electron interactions yielded results closest to experimental measurements. Using DFT-D3 method with Becke-Jonson damping, binding energies at different sites were estimated by performing indentation of water molecule onto silica slab. We determined the binding sites developing pure nonbonded interactions, using which interaction parameters between oxygen atoms of silica and water were calculated from potential energy curves. Using the estimated parameters for silica/water van der Waals interactions, we performed molecular dynamics simulations of water droplet on silica surface. Observed surface wetting recovered experimentally measured wetting behavior of silica with a water contact angle of approximately 12.4° on the flat and clean silica surface. Providing proper interaction parameters for the Lennard Jones model is an accurate and also simple alternative to existing complex surface interaction models.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Acknowledgements

This work was supported by the Scientific and Technological Research Council of Turkey (TÜBİTAK) under the Grant Number 217 M460. Authors would like to thank Center for Scientific Computation at Southern Methodist University. Dr. Barisik also thanks for the support from the Turkish Academy of Sciences (TUBA) in the framework of the Young Scientist Award Programme (GEBIP).

References

H.G. Ozcetik, et al.

Applied Surface Science 504 (2020) 144359


